



GCE AS MARKING SCHEME

SUMMER 2023

**AS
MATHEMATICS
UNIT 1 PURE MATHEMATICS A
2300U10-1**

INTRODUCTION

This marking scheme was used by WJEC for the 2023 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

GCE AS MATHEMATICS
UNIT 1 PURE MATHEMATICS A
SUMMER 2023 MARK SCHEME

Q Solution**Mark Notes**

1(a) $1 + {}^9C_1(-3x)^1 + {}^9C_2(-3x)^2$ B1 ${}^9C_1(-3x)^1$

B1 ${}^9C_2(\pm 3x)^2$, oe

$1 - 27x + 324x^2$ B1 cao Ignore extra terms

1(b) Put $x = 0.001$

M1 sub $x = 0.001$ into either side. si

$(1 - 3 \times 0.001)^9$

$= 1 - 27(0.001) + 324(0.001)^2$ A1 correct sub, ft their (a), for equivalent difficulty

$(0.997)^9 = 1 - 0.027 + 0.000324$

$(0.997)^9 = 0.973(324)$

$(0.997)^9 = 0.973$ to 3dp

A1 cao for their expression in (a), provided $0 < \text{answer} < 1$
3dp required

Q	Solution	Mark Notes
2	$3\sin^2 \theta - 5\cos^2 \theta = 2\cos \theta$	
	$3(1 - \cos^2 \theta) - 5\cos^2 \theta = 2\cos \theta$	M1 $\sin^2 \theta + \cos^2 \theta = 1$
	$8\cos^2 \theta + 2\cos \theta - 3 = 0$	
	$(2\cos \theta - 1)(4\cos \theta + 3) = 0$	m1 factorisation, oe
		$ax^2 + bx + c = (dx + e)(fx + g)$
		$df = a$ and $eg = c$
	$\cos \theta = \frac{1}{2}, -\frac{3}{4}$	A1
	$\cos \theta = \frac{1}{2}$	
	$\theta = 60^\circ$	B1 ft
	$\theta = 300^\circ$	B1 ft
	$\cos \theta = -\frac{3}{4}$	
	$\theta = 138.59^\circ$	B1 ft, Accept 139°
	$\theta = 221.41^\circ$	B1 ft, Accept 221°

Notes

Mark each branch separately.

FT 2 branches only if different signs.

For each branch, -1 for a 3rd root in the range $0^\circ < \theta < 360^\circ$,

-1 for a 4th root in the range $0^\circ < \theta < 360^\circ$.

Ignore roots outside the range $0^\circ < \theta < 360^\circ$.

Q	Solution	Mark Notes
3(a)	Gradient of $AB = \frac{8-5}{3-(-2)} \left(= \frac{3}{5} \right)$	B1
	Correct method for finding the equ AB	M1
	Equation of AB is $y - 5 = \frac{3}{5}(x - (-2))$	A1 or $y - 8 = \frac{3}{5}(x - 3)$ ft grad AB , any correct form. ISW
	$5y = 3x + 31$	
3(b)	Gradient $AC = -\frac{5}{3}$	M1 $-1/\text{grad } AB$, ft their grad AB
	Equation of AC is $y - 5 = -\frac{5}{3}(x - (-2))$	m1 correct method
	$3y + 5x = 5$	
	At C , $y = 0$, $5x = 5$, $x = 1$	
	C has coordinates $(1, 0)$	A1 Convincing

OR

Assuming that C is $(1, 0)$

$$\text{Gradient } AC = \frac{5-0}{-2-1} = -\frac{5}{3} \quad (\text{M1})$$

$$\text{Grad } AC \times \text{Grad } AB = -\frac{5}{3} \times \frac{3}{5} = -1 \quad (\text{m1})$$

Hence AC and AB are perpendicular (A1)

OR

$$\text{Gradient } AC = -\frac{5}{3} \quad (\text{M1}) \quad -1/\text{grad } AB$$

C has coordinates $(p, 0)$

$$\frac{5-0}{-2-p} = -\frac{5}{3} \quad (\text{m1})$$

$$15 = 10 + 5p, p = 1 \quad (\text{A1})$$

Q	Solution	Mark Notes
3(c)	$AB = \sqrt{(8 - 5)^2 + (3 + 2)^2} = \sqrt{34}$	M1 correct method for distance
	$AC = \sqrt{(0 - 5)^2 + (1 + 2)^2} = \sqrt{34}$	A1 one correct distance
	$\text{Area of } ABC = \frac{1}{2} \times AB \times AC$	M1 correct method for area used
	$\text{Area of } ABC = \frac{1}{2} \times \sqrt{34} \times \sqrt{34} = 17$	A1 cao

OR

Area ABC

$$\begin{aligned}
 &= \frac{1}{2}(5 + 8) \times (3 - (-2)) - \frac{1}{2} \times 3 \times 5 - \frac{1}{2} \times 8 \times 2 && \text{(M1)} \\
 &&& \text{(M1) correct area identified} \\
 &&& \text{(A1) correct expression} \\
 &= \frac{65}{2} - \frac{15}{2} - 8 \\
 &= 17 && \text{(A1) cao}
 \end{aligned}$$

OR

Triangle ABC is isosceles with $AC = AB$ and base $= BC$.

$$\text{Midpoint of base} = (2, 4) \quad \text{(M1)}$$

$$\begin{aligned}
 \text{Length of base}(BC) &= \sqrt{(3 - 1)^2 + (8 - 0)^2} \\
 &= 2\sqrt{17}
 \end{aligned}$$

$$\text{Height} = \sqrt{(2 - -2)^2 + (4 - 5)^2} = \sqrt{17} \quad \text{(A1) One correct length}$$

$$\begin{aligned}
 \text{Area of } ABC &= \frac{1}{2} \times \text{base} \times \text{height} && \text{(M1) correct method for area used} \\
 \text{Area of } ABC &= \frac{1}{2} \times 2\sqrt{17} \times \sqrt{17} \\
 &= 17 && \text{(A1) cao}
 \end{aligned}$$

Q	Solution	Mark Notes
3(d)	BC is diameter of required circle	M1 si
	Method to find the centre	M1
	$\text{Centre} = \left(\frac{3+1}{2}, \frac{8+0}{2} \right)$	
	$\text{Centre} = (2, 4)$	
	Method to find the radius	M1 from same diameter
	$\text{Radius} = \frac{1}{2} \sqrt{8^2 + 2^2}$	$\sqrt{4^2 + 1^2}$, or radius ²
	$\text{Radius} = \sqrt{17}$	
	Method for the equation of a circle	m1 Dependent on all previous 3 M1s
	$(x - 2)^2 + (y - 4)^2 = 17$	A1 oe, cao, ISW

OR

Equation of circle is $x^2 + y^2 + ax + by + c = 0$ (M1)	used, or $(x - p)^2 + (y - q)^2 = r^2$
For $C(1, 0)$, $a + c = -1$	(A1) one correct equation
For $A(-2, 5)$, $-2a + 5b + c = -4 - 25$	
For $B(3, 8)$, $3a + 8b + c = -9 - 64$	(A1) 3 correct equations
Correct method for solving equations	(M1)
$a = -4, b = -8, c = 3$	(A1) cao
$x^2 + y^2 - 4x - 8y + 3 = 0$	

Q Solution **Mark Notes**

4(a)	Attempt at long division	M1	oe, si
	$3x^2 + 11x (+ 34)$	A1	implied by 101
	Remainder = 101	A1	cao
4(b)(i)	Attempt to use $f(-2) = 0$.	M1	
	$f(-2) = 2(-2)^3 - 3(-2)^2 + a(-2) + 6 = 0$	A1	correct equation, si
	$a = -11$	A1	

Q	Solution	Mark Notes
4(b)(ii)	$f(x) = (x + 2)(2x^2 + px + q)$	M1 at least one of p, q correct, ft if poss. oe
	$f(x) = (x + 2)(2x^2 - 7x + 3)$	A1
	$f(x) = (x + 2)(2x - 1)(x - 3)$	
	$x = -2$	
	$x = \frac{1}{2}$	A1 or $x = 3$
	$x = 3$	A1 all three roots

OR

Use of factor theorem where $x \neq -2$	(M1)
1 st correct root $\neq -2$	(A1)
2 nd correct root $\neq -2$	(A1)
All three roots	(A1)

OR for (b)(i) and (b)(ii)

$2x^3 - 3x^2 + ax + 6 = (x + 2)(2x^2 + px + q)$	(M1)
Comparing coefficients	(M1)
For x^2 : $-3 = 4 + p$; $p = -7$	(A1)
constant term $6 = 2q$; $q = 3$	(A1)
$f(x) = (x + 2)(2x^2 - 7x + 3)$	$(x - 3)(2x^2 + 3x - 2)$, $(2x - 1)(x^2 - x - 6)$
$f(x) = 2x^3 - 3x^2 - 11x + 6$	
$a = -11$	(A1)
$f(x) = (x + 2)(2x - 1)(x - 3)$	(A1)
$x = -2, \frac{1}{2}, 3$	(A1)

Q Solution**Mark Notes**

$$5 \quad \frac{\sqrt[3]{512a^2} - \frac{\frac{7}{6} \times a^{-\frac{1}{3}}}{a^{\frac{1}{6}}}}{a^{\frac{1}{6}}}$$

$$\sqrt[3]{512a^2} = 8a^{\frac{2}{3}}$$

B1 oe

$$\frac{\frac{7}{6} \times a^{-\frac{1}{3}}}{a^{\frac{1}{6}}} = a^{\left(\frac{7}{6} - \frac{1}{3} - \frac{1}{6}\right)}$$

B1 some correct simplification of indices

$$= a^{\frac{2}{3}}$$

B1 2nd term correct, oe

$$\sqrt[3]{512a^2} - \frac{\frac{7}{6} \times a^{-\frac{1}{3}}}{a^{\frac{1}{6}}} = 8a^{\frac{2}{3}} - a^{\frac{2}{3}}$$

$$= 7a^{\frac{2}{3}} \quad \text{or} \quad 7\sqrt[3]{a^2}$$

B1 cao

Q	Solution	Mark Notes
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6 Cosine rule used correctly M1

$$AC^2 = AB^2 + BC^2 - 2(AB)(BC)\cos B$$

$$(4 + \sqrt{3})^2 = (3)^2 + (2\sqrt{5})^2 - 2(3)(2\sqrt{5})\cos B \quad \text{A1} \quad \text{All correct}$$

$$19 + 8\sqrt{3} = 9 + 20 - 12\sqrt{5} \cos B \quad \text{B1} \quad 16 + 8\sqrt{3} + 3$$

$$\text{B1} \quad 9 \text{ and } 20$$

$$\text{B1} \quad 12\sqrt{5}$$

$$12\sqrt{5} \cos B = 10 - 8\sqrt{3}$$

$$\cos B = \frac{10 - 8\sqrt{3}}{12\sqrt{5}}$$

$$\cos B = \frac{5 - 4\sqrt{3}}{6\sqrt{5}} \quad \text{A1} \quad a = 5$$

$$\text{A1} \quad b = 4$$

If A0A0, award A1 for $\cos B = \frac{10 - 8\sqrt{3}}{12\sqrt{5}}$ or

$$\cos B = \frac{-10 + 8\sqrt{3}}{-12\sqrt{5}}$$

ISW

Q	Solution	Mark Notes
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7(a)(i) $2x^2 + 5x - 12 = mx - 14$	M1
$2x^2 + (5 - m)x + 2 = 0$	A1 Allow $2x^2 + 5x - mx + 2 = 0$
Discriminant = $(5 - m)^2 - 4 \times 2 \times 2$	m1 si
For tangent discriminant = 0	m1 used
$25 - 10m + m^2 - 16 = 0$	
$m^2 - 10m + 9 = 0$	A1 convincing

7(a)(ii) $(m - 1)(m - 9) = 0$	oe $(5 - m) = \pm 4$
$m = 1, 9$	B1B1
When $m = 1$	when $m = 9$
$2x^2 + 5x - 12 = x - 14$ or $2x^2 + 5x - 12 = 9x - 14$	B1
$2x^2 + 4x + 2 = 0$ or $2x^2 - 4x + 2 = 0$	
$(x + 1)^2 = 0$ or $(x - 1)^2 = 0$	B1 si
$x = -1$ and $x = 1$	B1 or $(-1, -15)$ or $(1, -5)$
$y = -15$ and $y = -5$	
Points are $(-1, -15)$ and $(1, -5)$	B1 2 nd correct pair

OR for final 4 B1 marks

$m = 1, \frac{dy}{dx} = 4x + 5 = 1 \quad (x = -1)$	(B1)
$m = 9, \frac{dy}{dx} = 4x + 5 = 9 \quad (x = 1)$	(B1)
$x = -1$ and $x = 1$	(B1) or $(-1, -15)$ or $(1, -5)$
$y = -15$ and $y = -5$	
Points are $(-1, -15)$ and $(1, -5)$	(B1) 2 nd correct pair

Q Solution**Mark Notes**Alternative solution for Q7 (using the gradient function)

7(a)(i) At point of intersection

$$2x^2 + 5x - 12 = mx - 14 \quad (\text{M1})$$

$$\text{Gradient of curve} = \frac{dy}{dx} = 4x + 5 \quad (\text{m1})$$

$$\text{When line is tangent, } 4x + 5 = m \quad (\text{A1})$$

$$x = \frac{m-5}{4}$$

$$2\left(\frac{m-5}{4}\right)^2 + 5\left(\frac{m-5}{4}\right) - 12 = m\left(\frac{m-5}{4}\right) - 14 \quad (\text{A1})$$

$$m^2 - 10m + 9 = 0 \quad (\text{A1}) \quad \text{convincing}$$

7(a)(ii) $2x^2 + 5x - 12 = mx - 14 \quad (\text{M1})$

$$\text{At point of contact, } m = 4x + 5 \quad (\text{A1})$$

$$2x^2 + 5x - 12 = (4x + 5)x - 14 \quad (\text{m1})$$

$$2x^2 - 2 = 0$$

$$(x + 1)(x - 1) = 0 \quad (\text{m1}) \quad \text{or } x^2 = 1$$

$$x = -1, 1 \quad (\text{A1}) \quad \text{one correct pair}$$

$$y = -15, -5 \quad (\text{A1}) \quad \text{all correct}$$

7(b) For 2 distinct points of intersection

$$\text{Discriminant} > 0 \quad \text{M1} \quad \text{used, si}$$

$$(m - 1)(m - 9) > 0 \quad \text{OR } 5 - m > 4 \text{ or } 5 - m < -4$$

$$m < 1 \text{ or } m > 9 \quad \text{A1} \quad \text{condone ',', or nothing}$$

A0 for 'and'

A0 for non-strict inequality

Mark final answer

Q	Solution	Mark Notes
8	$n = 3$ $n^2 + 1 = 3^2 + 1 = 10$ 10 ($= 2 \times 5$) is not a prime number, hence the statement is false.	M1 correct value of n (e.g. 5, 7, 8) A1 correct value (e.g. 26, 50, 65) A1 concluding statement Condone one of 'statement is false' or e.g. '10 is not a prime number'

Q	Solution	Mark Notes
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9(a) $y + \delta y = (x + \delta x)^2 - 3(x + \delta x)$ B1

$$y + \delta y = x^2 + 2x(\delta x) + (\delta x)^2 - 3x - 3\delta x$$

Subtract $y = x^2 - 3x$ from $y + \delta y$ M1

$$\delta y = 2x\delta x + (\delta x)^2 - 3\delta x$$
 A1

$$\frac{\delta y}{\delta x} = 2x + \delta x - 3$$

$$\frac{dy}{dx} = \lim_{\delta x \rightarrow 0} \frac{\delta y}{\delta x}$$
 M1
$$\frac{dy}{dx} = \lim_{\delta x \rightarrow 0} (2x + \delta x - 3)$$

$$\frac{dy}{dx} = 2x - 3$$
 A1 All correct

OR

$$f(x + h) = (x + h)^2 - 3(x + h)$$
 (B1)

$$f(x + h) = x^2 + 2xh + h^2 - 3x - 3h$$

$$f(x + h) - f(x) = 2xh + h^2 - 3h$$
 (M1A1)

$$\frac{f(x+h)-f(x)}{h} = 2x + h - 3$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h)-f(x)}{h}$$
 (M1)
$$f'(x) = \lim_{h \rightarrow 0} (2x + h - 3)$$

$$f'(x) = 2x - 3$$
 (A1) All correct

Q Solution**Mark Notes**

$$9(b)(i) f(x) = 4x^{\frac{3}{2}} + \frac{6}{\sqrt{x}}$$

$$f'(x) = 4 \times \frac{3}{2} \times x^{\frac{1}{2}} + 6 \times \left(-\frac{1}{2}\right) \times x^{-\frac{3}{2}}$$

B1 one correct term

B1 second correct term
ISW

$$f'(x) = 6x^{\frac{1}{2}} - 3x^{-\frac{3}{2}}$$

$$9(b)(ii) f'(x) > 0$$

$$6x^{\frac{1}{2}} - 3x^{-\frac{3}{2}} > 0$$

$$\text{Multiplying by } x^{\frac{3}{2}}: 6x^2 - 3x^0 > 0$$

M1 oe eg $3x^{\frac{1}{2}}(2 - x^{-2})$ FT similar expression
Allow $\leq, <, =, \geq$

$$x^2 > 0.5$$

A1 Allow $\leq, <, =, \geq$, but must be same as
in previous M1
FT similar expression

$$\text{For increasing function } f'(x) > 0$$

M1 used
Allow $f'(x) \geq 0$

$$x > (0.5)^{\frac{1}{2}} = 0.707106.....$$

$$k = 0.71$$

A1 cao needs 2 dp
Condone $x = 0.71$

Q Solution**Mark Notes**

10(a) $2x + 5 = e^3$

M1 Correctly removing \ln

$$x = \frac{1}{2}(e^3 - 5) (= 7.5427\dots)$$

A1 ISW, Accept 7.54
Answer only, M0

10(b) $(2x + 1)\ln 5 = \ln 14$

M1 oe $2x\ln 5 = \ln\left(\frac{14}{5}\right)$

$$2x = \frac{\ln 14}{\ln 5} - 1$$

A1 isolating x term

$$x = \frac{1}{2}\left(\frac{\ln 14}{\ln 5} - 1\right) (= 0.31(98\dots))$$

A1 ISW, Accept 0.32
Answer only, M0

OR

$$2x + 1 = \log_5 14$$

(M1)

$$2x = \log_5 14 - 1$$

(A1) isolating x term

$$x = \frac{1}{2}(\log_5 14 - 1) (= 0.31(98\dots))$$

(A1) ISW, Accept 0.32
Answer only, M0

10(c) $\log_7\left(\frac{8x^3 \times x}{8x^2}\right) = 4$

B1 one use power law

B1 one use addition law

B1 one use subtraction law

B1 $\log_3 81 = 4$, si

$$\log_7 x^2 = 4, 2\log_7 x = 4$$

$$\log_7 x = 2$$

B1 $x^2 = 7^4$

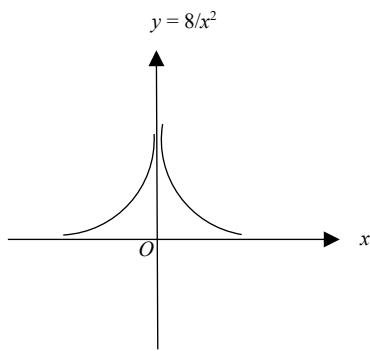
$$x = 49$$

B1 B0 for ± 49

Q Solution

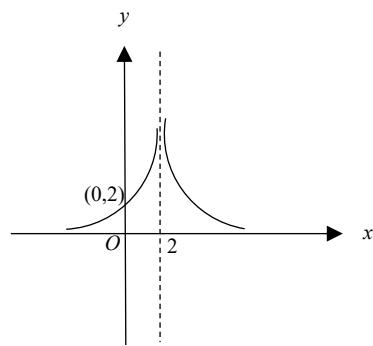
Mark Notes

11(a)



B2 B1 each branch

11(b)

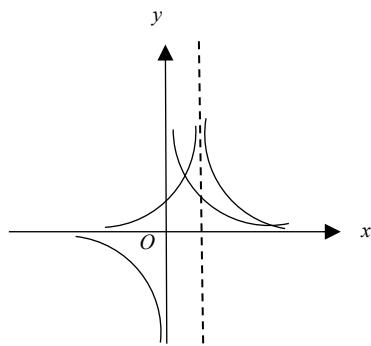


M1 ft shift entire graph to the right

B1 $(0, 2)$ caoA1 $x = 2$ as **asymptote**

Q Solution**Mark Notes**

11(c)



Equation has two solutions

B1 correct curve $y = \frac{8}{x}$, both branches.

May be seen in (b).

B1 award only if both graphs correct in first quadrant.

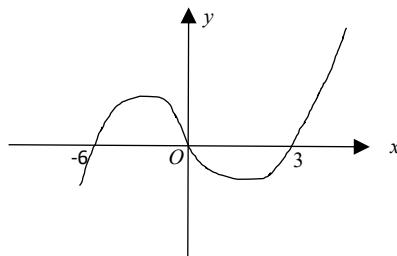
Q	Solution	Mark Notes
12(a) $\mathbf{AB} = \mathbf{b} - \mathbf{a}$		M1 used
$\mathbf{AB} = 8\mathbf{i} + 4\mathbf{j}$		A1 any notation ISW
12(b)(i) $ \mathbf{a} = \sqrt{(-3)^2 + 4^2} = 5$		B1 si
Unit vector = $-\frac{3}{5}\mathbf{i} + \frac{4}{5}\mathbf{j}$		B1 oe
12(b)(ii) Position vector of C is $7\left(-\frac{3}{5}\mathbf{i} + \frac{4}{5}\mathbf{j}\right)$		B1 oe, ft from (b)(i), provided vector is not \mathbf{a} , \mathbf{b} or \mathbf{AB} .
$= \left(-\frac{21}{5}\mathbf{i} + \frac{28}{5}\mathbf{j}\right)$		
12(c) $AOB = 180^\circ - \tan^{-1}\left(\frac{8}{5}\right) - \tan^{-1}\left(\frac{4}{3}\right)$		M1 oe
$AOB = 180^\circ - 57.99^\circ - 53.13^\circ$		B1 any correct relevant angle, si
$AOB = 68.9^\circ \ (68.875\dots)$		A1
OR		
angle $AOB = \tan^{-1}\left(\frac{5}{8}\right) + \tan^{-1}\left(\frac{3}{4}\right)$		(M1) oe
angle $AOB = 32.01^\circ + 36.87^\circ$		(B1) any correct relevant angle, si
angle $AOB = 68.9^\circ \ (68.875\dots)$		(A1)
OR		
$OA = \sqrt{(-3)^2 + 4^2} = \sqrt{25}$		
$OB = \sqrt{5^2 + 8^2} = \sqrt{89}$		
$AB = \sqrt{8^2 + 4^2} = \sqrt{80}$		(B1) all correct
$80 = 25 + 89 - 2 \times 5 \times \sqrt{89} \cos\theta$		(M1) correct use of cosine rule with their distances
$\cos\theta = \frac{25 + 89 - 80}{10\sqrt{89}} = 0.3603992792$		
angle $AOB = 68.9^\circ \ (68.875\dots)$		(A1)

Q Solution

13(a) $4\frac{x^{\frac{1}{3}}}{\frac{1}{3}} + \frac{5}{4}x^4 + 7x + C$

Mark NotesB3 B1 each term ISW
-1 if no $+C$

13(b)

Curve cuts x -axis when $x = -6, 0, 3$ B1 maybe seen on sketch,
may be implied by limits

$$f(x) = x^3 + 3x^2 - 18x$$

B1

$$A_1 = \int_{-6}^0 (x^3 + 3x^2 - 18x) dx$$

M1 attempt to integrate, limits not required.

$$= \left[\frac{x^4}{4} + x^3 - 9x^2 \right]_{-6}^0$$

A1 correct integration,
ft similar expression,
limits not required

$$= (0) - \left(\frac{(-6)^4}{4} + (-6)^3 - 9 \times (-6)^2 \right)$$

m1 correct use of limits, either -6 and 0,
or 0 and 3

$$= 216$$

A1 Must be from -6 to 0
Only FT for
 $f(x) = x^3 - 3x^2 - 18x$
 $\left(\int_{-6}^0 f(x) dx = -216 \right)$
or $f(x) = x^3 + 3x^2 + 18x$
 $\left(\int_{-6}^0 f(x) dx = -432 \right)$

Q Solution**Mark Notes**

13(b) (continued)

$$\begin{aligned}
 A_2 &= \left[\frac{x^4}{4} + x^3 - 9x^2 \right]_0^3 \\
 &= \left(\frac{3^4}{4} + 3^3 - 9 \times 3^2 \right) - (0) \\
 &= -\frac{135}{4} = -33.75
 \end{aligned}$$

A1 allow (+)33.75,

Only FT for
 $f(x) = x^3 - 3x^2 - 18x$
 $\left(\int_0^3 f(x) dx = -87.75 \right)$
 or $f(x) = x^3 + 3x^2 + 18x$
 $\left(\int_0^3 f(x) dx = 128.25 \right)$

Total area = $216 + \frac{135}{4}$

m1 si

Total area = $\frac{999}{4} = 249.75$

A1 cao

Note:

Must be supported by workings.

If M0, award SC1 for sight of 216 **and** ± 33.75 , **OR** SC2 for 249.75

Q Solution**Mark Notes**

14(a) $y = Ae^{-kx}$ or $y = Ae^{kx}$

B1 oe Accept numerical values for $A \neq 0$, and/or $k \neq 0$.

14(b)(i) $Y = 5e^{-kt}$

B1 for $A = 5$

$$1.25 = 5e^{-4k}$$

$$e^{-4k} = 0.25$$

$$k = -\frac{1}{4}\ln(0.25) = 0.3465(735903)$$

B1 Convincing, answer given
Allow verification

14(b)(ii) $0.6 = 5e^{-0.3466t}$

M1

$$e^{-0.3466t} = 0.12$$

$$t = \frac{\ln(0.12)}{-0.3466} (= 6.12 \text{ (hours)})$$

A1

Additional time ($= 6.12 - 4$) = 2.12 (hours) A1

oe e.g. hours and minutes, ISW
Award A1 for “their 6.12” – 4,
provided “their 6.12” > 4